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Journal Watch

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# Exploiting Sparsity in Tight-Dimensional Spaces for Piecewise Continuous Signal Recovery

Hiroki Kuroda, Masao Yamagishi and  
Isao Yamada

# Sparsity Piecewise Continuous Signal Recovery

$s(t|\mathbf{C}^*, \mathbf{p}^*)$

$$:= \begin{cases} \sum_{k=1}^K [\mathbf{C}^*]_{k,1} \varphi_k(t), & (t \in (-\infty, [\mathbf{p}^*]_1)), \\ \vdots & \\ \sum_{k=1}^K [\mathbf{C}^*]_{k,\ell} \varphi_k(t), & (t \in [[\mathbf{p}^*]_{\ell-1}, [\mathbf{p}^*]_{\ell})), \\ \vdots & \\ \sum_{k=1}^K [\mathbf{C}^*]_{k,L+1} \varphi_k(t), & (t \in [[\mathbf{p}^*]_L, \infty)), \end{cases}$$

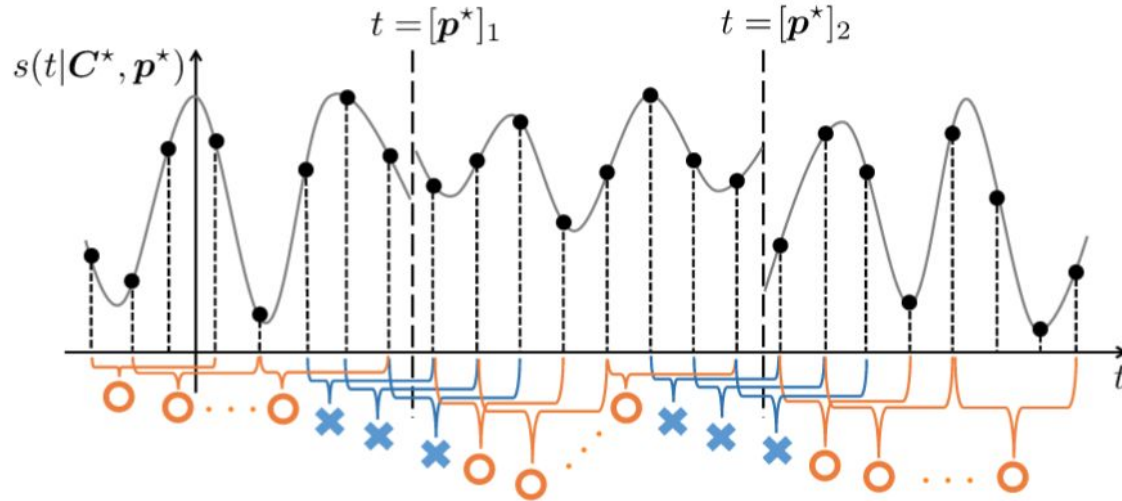
Measurement model: Linear and Noisy

Obtain  $\hat{\mathbf{s}} \approx \mathbf{s}^*$

Obtain  $\hat{\mathbf{p}} \approx \mathbf{p}^*$

Obtain  $\hat{\mathbf{C}} \approx \mathbf{C}^*$

# Sparsity Piecewise Continuous Signal Recovery



1. Design  $\mathbf{W}$  such that  $\mathbf{W}\mathbf{s}^*$  is sparse
2. Identify  $\mathbf{p}^*$
3. Estimate  $\mathbf{C}^*$  using least squares

# Detection Theory for Union of Subspaces

Muhammad Asad Lodhi, Waheed U.  
Bajwa



# Detection Theory for Union of Subspaces

- Model

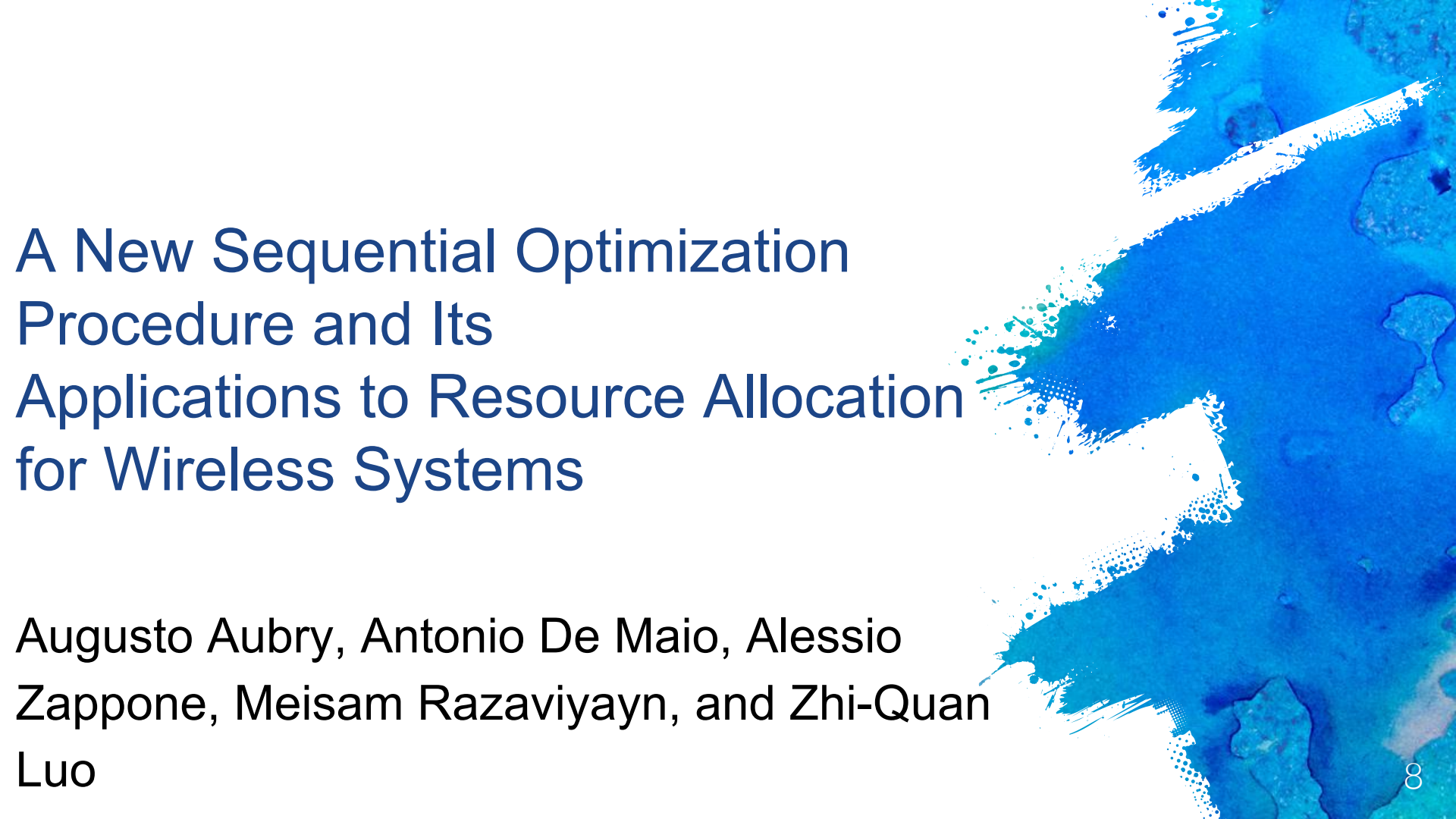
$$\mathcal{H}_0 : \mathbf{y} = \mathbf{n};$$

$$\mathcal{H}_k : \mathbf{y} = \mathbf{x} + \mathbf{n}, \mathbf{x} \in S_k; \quad k = 1, \dots, K_0.$$

- Problem 1: signal detection
- Problem 2: active subspace detection
- Generalized likelihood ratio tests for detection (GLRT)

# Detection Theory for Union of Subspaces

- Analysis: Colored Gaussian noise with full rank covariance matrix
  - Known noise statistics
  - Unknown variance, known correlation
  - Unknown variance, known correlation
- Performance metric: probabilities of
  - Detection
  - Classification
  - False alarm



# A New Sequential Optimization Procedure and Its Applications to Resource Allocation for Wireless Systems

Augusto Aubry, Antonio De Maio, Alessio  
Zappone, Meisam Razaviyayn, and Zhi-Quan  
Luo



# Sequential Optimization Procedure

$$\begin{aligned} \max_{\mathbf{x}_1, \dots, \mathbf{x}_K} \quad & f(\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_K) \\ \text{s.t.} \quad & \phi_{i,h}(\mathbf{x}_h) \geq 0, \quad h = 1, 2, \dots, K \\ & \quad \quad \quad i = 1, \dots, K_{1,h} \end{aligned}$$

- Existing ideas
  - Alternating minimization
  - Maximum block improvement (MBI)
- Proposal: Join MBI and sequential method

$$\begin{aligned} \tilde{\phi}_{i,h}(\mathbf{y}; \mathbf{x}_h) &\leq \phi_{i,h}(\mathbf{y}), \quad \forall i = 1, \dots, K_{1,h}; \\ \tilde{\phi}_{i,h}(\mathbf{x}_h; \mathbf{x}_h) &= \phi_{i,h}(\mathbf{x}_h), \quad \forall i = 1, \dots, K_{1,h}. \end{aligned}$$

# Sequential Optimization Procedure

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- 1: **Input:** A feasible starting point  $\mathbf{x}^{(0)} = (\mathbf{x}_1^{(0)}, \dots, \mathbf{x}_K^{(0)})$ .
- 2: set  $n = 1$ .
- 3: **repeat**
- 4: for  $h = 1, 2, \dots, K$ , let  $\nu_h^{(n)}$  and  $\mathbf{y}_h^{(n)}$  be, respectively, the optimal value and an optimal solution to problem

$$\mathcal{P}_{(\mathbf{x}^{(n-1)})}^h \begin{cases} \max_{\mathbf{y}} f_h(\mathbf{y}; \mathbf{x}^{(n-1)}) \\ \text{s.t. } \tilde{\phi}_{i,h}(\mathbf{y}; \mathbf{x}_h^{(n-1)}) \geq 0, h = 1, 2, \dots, K, \\ i = 1, \dots, K_{1,h} \end{cases}$$

- 5: Let  $k^* = \arg \max_{k=1,2,\dots,K} \nu_k^{(n)}$ . Define  $\mathbf{x}_h^{(n)} = \mathbf{x}_h^{(n-1)}$  for all  $h \neq k^*$  and  $\mathbf{x}_{k^*}^{(n)} = \mathbf{y}_{k^*}^{(n)}$ , i.e.,

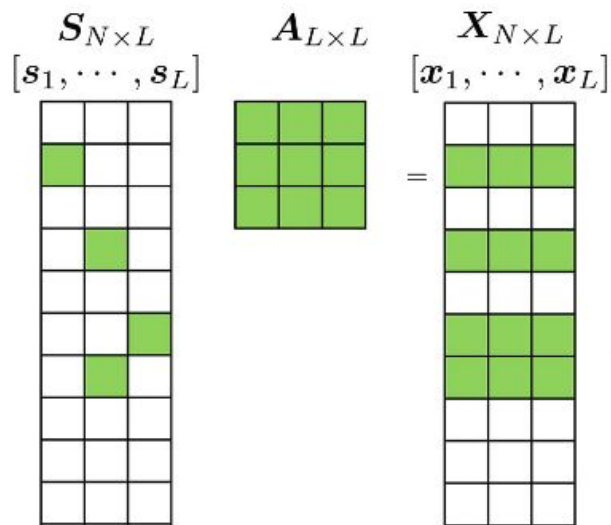
$$\mathbf{x}^{(n)} = \left[ \mathbf{x}_1^{(n-1)}, \dots, \mathbf{x}_{k^*-1}^{(n-1)}, \mathbf{y}_{k^*}^{(n)}, \mathbf{x}_{k^*+1}^{(n-1)}, \dots, \mathbf{x}_K^{(n-1)} \right]^T ;$$

- 6: **until** Convergence
  - 7: **Output:**  $\mathbf{x}_h^* = \mathbf{x}_h^{(n)}$ ,  $h = 1, 2, \dots, K$ .
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# A Recovery of Independent Sparse Sources From Linear Mixtures Using Sparse Bayesian Learning

Seyyed Hamed Fouladi, Sung-En Chiu,  
Bhaskar D. Rao, and Ilanko  
Balasingham

# Recovery of Independent Sparse Sources From Linear Mixtures



$$Y = \Phi X, \quad X = SA.$$

$$\min_{S, A} \sum_{i=1}^L \|s_i\|_0, \quad \text{subject to } Y = \Phi SA, \quad X = SA$$

$$\text{and } \sqrt{\sum_{j=1}^L (A_{(i,j)})^2} = 1. \quad ($$



# Recovery of Independent Sparse Sources From Linear Mixtures

- Uniqueness conditions

$$\max_i \{r_i\} + \sum_{j=1}^L r_j < \text{Spark}(\Phi).$$

- SBL-based recovery algorithm
  - Hyperparameters:  $\Theta = \{\Gamma, \sigma^2, \mathbf{A}\}$
  - Closed form expressions for EM updates
- Analysis of global minima and local minima of SBL cost function



# Other Interesting Papers

- **Discreteness-Aware Approximate Message Passing for Discrete-Valued Vector Reconstruction**
  - R. Hayakawa and K. Hayashi
- **Bayesian Detection for MIMO Radar in Gaussian Clutter**
  - J. Liu, J. Han, Z.-J. Zhang, and J. Li
- **Source Counting and Separation Based on Simplex Analysis**
  - B. Laufer-Goldshtein, R. Talmon, and S. Gannot



A close-up photograph of a person's hands holding a lit sparkler. The sparkler is bright and glowing, with many sparks flying out. The person is wearing a grey, textured sweater. The background is white, and there is a dark, splattered circular border around the image.

**Thank You!** 🙏