

# Journal Watch

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# 1. Energy Harvesting Communication Using Finite-Capacity Batteries With Internal Resistance

Authors: Rajshekhar Vishweshwar Bhat, Mehul Motani, and Teng Joon Lim

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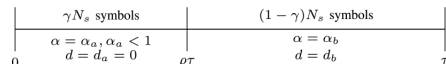
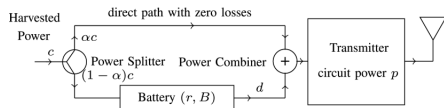


Figure: Frame structure

Figure: Dual path communication

- Maximum achievable rate for TX over an AWGN channel with gain  $h$ , symbol energy  $P$ , and unit received noise PSD is  $\mathbf{R} = \mathbf{log}(1 + \mathbf{hP})$  bits per channel symbol.

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$$R_{\text{avg}}(\boldsymbol{\rho}, \boldsymbol{\alpha}_a, \boldsymbol{\alpha}_b, \boldsymbol{\gamma}, \mathbf{d}_b) = \frac{1}{N} \sum_{i=1}^N R(\rho_i, \alpha_{a_i}, \alpha_{b_i}, \gamma_i, d_{b_i})$$



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- **Optimal Online Policy:** Stochastic dynamic programming, where state in frame  $n$  is  $s_n = (C_n, H_n, B_{n-1})$

$$\mathcal{R}_{\text{on}}^* = \max_{\pi \in \Pi} \frac{1}{N} \sum_{n=1}^N \mathbb{E} [R(C_n, H_n, B_{n-1}, \rho_n, \alpha_{a_n}, \alpha_{b_n}, d_{b_n}) | s_1, \pi]$$

## Offline single frame rate optimization problem:

$$P0 : \underset{\rho, \alpha_a, \alpha_b, \gamma, d_b}{\text{maximize}} R(\rho, \alpha_a, \alpha_b, \gamma, d_b) \quad (1a)$$

$$\text{subject to } (\tilde{d}_b - \tilde{c}_b)(1 - \rho)\tau - B_{\rho\tau} - B_0 \leq 0 \quad (1b)$$

$$B_0 + B_{\rho\tau} - (\tilde{d}_b - \tilde{c}_b)(1 - \rho)\tau - B \leq 0 \quad (1c)$$

$$0 \leq \rho \leq 1 \quad (1d)$$

$$\alpha_c \leq \alpha_a, \alpha_b \leq 1 \quad (1e)$$

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**Objective:** Optimize time and power splitting ratios

- Through an offline policy, assuming non-causal knowledge of harvested power and fading channel gains.
- Through sub-optimal policies when only statistics of energy arrivals and channel gains are known.

## Contributions:

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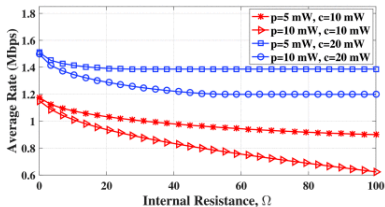
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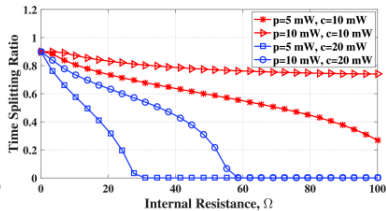
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- Solve for the optimal online policy by using stochastic dynamic programming. Also, propose three sub-optimal on-line algorithms which are practically feasible.
- Show via numerical simulations that the optimal policy designed for an ideal battery performs poorly when the internal resistance is not negligible



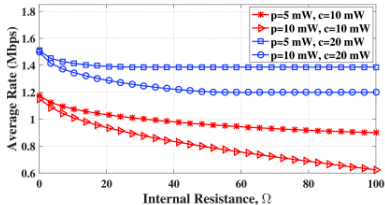


(a) Optimal Rate for the Single Frame

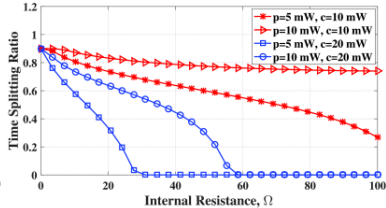


(b) Optimal Time Splitting Ratio for the Single Frame

Figure: Optimal rate and time splitting ratios

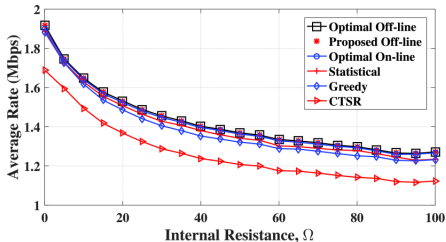
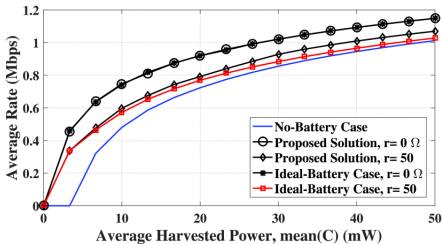


(a) Optimal Rate for the Single Frame



(b) Optimal Time Splitting Ratio for the Single Frame

Figure: Optimal rate and time splitting ratios



## 2. Online Ski Rental for ON/OFF Scheduling of Energy Harvesting Base Stations

Authors: Gilsoo Lee, Walid Saad, Mehdi Bennis, and Fumiyuki Adachi

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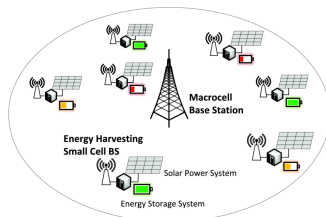
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## Approach:

- The operational cost of the BSs are computed in terms of transmission delay and energy consumption
- The original problem is decomposed into a set of distributed online optimization problems that are run at each SBS.
- The resulting problem is solved by a novel approach based on the ski rental problem. DOA (benchmark) and ROA (practical) are the two schemes used.

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## Assumptions:

- SBSs and the MBS will use different frequency bands.
- Each UE can be connected with only one of the BSs at a certain time  $t$  within a period of  $T$ .
- Energy harvesting is assumed to be done irrespective of whether an SBS is turned ON or OFF.

- State of BS

$$\sigma_j(t) = \begin{cases} 1, & \text{if SBS } j \text{ is turned ON at time } t, \\ 0, & \text{otherwise.} \end{cases} \quad (1)$$



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- Network Performance between UE  $i$  and SBS  $j$

$$\gamma_{ij}(\boldsymbol{\sigma}(t)) = \frac{P_j^{\text{tx}} \sigma_j(t) h_{ij}}{\sum_{j' \in \mathcal{B}^{\text{on}} \setminus \{j\}} P_{j'}^{\text{tx}} \sigma_{j'}(t) h_{ij'} + \rho^2} \quad (2)$$

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- Achievable data rate of UE  $i$

$$c_{ij}(\boldsymbol{\sigma}(t)) = \frac{B}{|\mathcal{I}_j(t)|} \log_2(1 + \gamma_{ij}(\boldsymbol{\sigma}(t))) \quad (3)$$

- **Transmission Delay:**

For TX  $K$  bits b/w BS  $j$ , UE in  $\mathcal{I}_j(t)$  at time  $t$ :

$$\phi_j(\boldsymbol{\sigma}(t)) = \sum_{i \in \mathcal{I}_j(\boldsymbol{\sigma}(t))} \frac{K}{c_{ij}(\boldsymbol{\sigma}(t))}. \quad (4)$$

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- **Power Consumption:**

$$\psi_j(\boldsymbol{\sigma}(t)) = \frac{|\mathcal{I}_j(\boldsymbol{\sigma}(t))|}{M} (1 - q) P_j^{\text{op}} + q P_j^{\text{op}} \quad (5)$$

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- **Operational Expenditure of SBS:**

$$r_j(\boldsymbol{\sigma}(t)) = \alpha_D \phi_j(\boldsymbol{\sigma}(t)) + \alpha_P \psi_j(\boldsymbol{\sigma}(t)), \quad (6)$$

- The Operational Expenditure of MBS (worst case) can be divided into per-SBS costs

$$\Phi_0^{\mathcal{I}_j(0)} = \sum_{i \in \mathcal{I}_j(0)} \frac{K}{\frac{B_m}{I} \log_2(1 + \gamma_{i0}(0))}. \quad (7)$$

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- Operational SBS Penalty / MBS expenditure:**

$$b_j = \alpha_B \left( \alpha_D \Phi_0^{\mathcal{I}_j(\sigma(0))} + \alpha_P \Psi_0^{\mathcal{I}_j(\sigma(0))} \right) T \quad (9)$$

- ON/OFF Scheduling as an Online Optimization Problem

$$\min_{\sigma(t), x} \sum_{j=1}^J \left( \int_0^{u_j} r_j(\sigma(\tau)) \sigma_j(\tau) d\tau + b_j x_j \right), \quad (10)$$

$$\begin{aligned} \text{s.t. } \sigma_j(t) + x_j &\geq 1, & 0 \leq t \leq u_j, & \forall j, \\ \sigma_j(t) &\in \{0, 1\}, & 0 \leq t \leq u_j, & \forall j, \\ x_j &\in \{0, 1\}, & \forall j \end{aligned}$$

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- Proposition - (10) can be decomposed into  $j$  subproblems

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- Competitive ratio** of an online algorithm is defined by

$$\kappa = \max_{u_j} \frac{\beta_{\text{ALG}}(u_j)}{\beta_{\text{OPT}}(u_j)}, \quad \forall u_j, \quad (12)$$

- **Online ski rental:**

$$\beta_{\text{OPT}}(u_j) = \begin{cases} r_j u_j, & 0 \leq u_j \leq \frac{b_j}{r_j}, \\ b_j, & \frac{b_j}{r_j} \leq u_j \leq T. \end{cases} \quad (13)$$

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- **DOA:** SBS  $j$  is turned OFF at a predetermined time  $t_j$ ,  $0 \leq t_j \leq T$

$$\frac{\beta_{\text{DOA}}(u_j)}{\beta_{\text{OPT}}(u_j)} = \begin{cases} \frac{r_j u_j}{\min\{r_j u_j, b_j\}}, & 0 \leq u_j \leq t_j, \\ \frac{r_j t_j + b_j}{\min\{r_j u_j, b_j\}}, & t_j \leq u_j \leq T, \end{cases} \quad (14)$$

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- **ROA:**  $\kappa$  is minimized to  $\frac{e}{e-1} = 1.86$



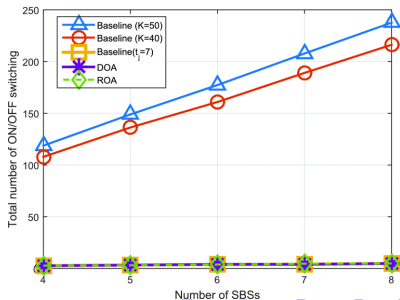
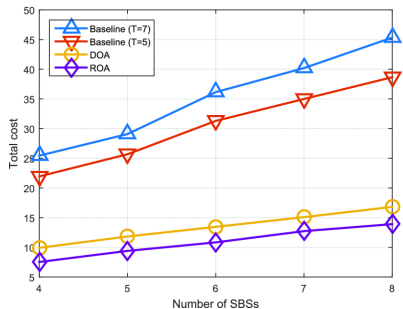
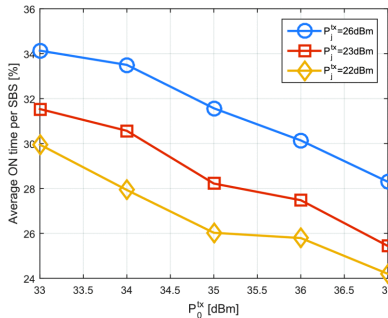
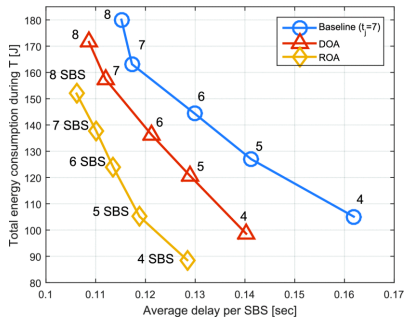
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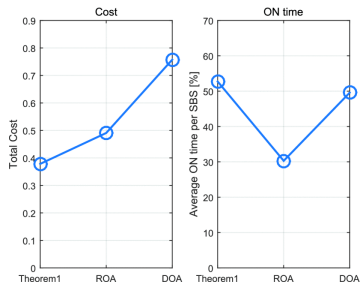
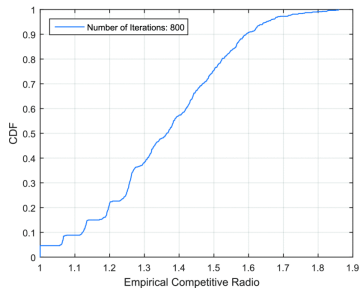
- Novel approach to optimize the ON/OFF schedule of self-powered SBSs, formulating the problem as one of minimizing network operational costs during a period.
- Proposed DOA, ROA is shown to achieve the optimal competitive ratio for the approximated problem. Using the proposed ROA, each SBS can autonomously decide on its ON time without prior information on future energy arrivals.
- Simulation results show that both delay and ON/OFF switching overhead are significantly reduced when one adopts the online ski rental approach.

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- Proposed DOA, ROA is shown to achieve the optimal competitive ratio for the approximated problem. Using the proposed ROA, each SBS can autonomously decide on its ON time without prior information on future energy arrivals.
- Simulation results show that both delay and ON/OFF switching overhead are significantly reduced when one adopts the online ski rental approach.

**Numerical result:** Compared with a baseline approach, ROA can yield performance gains reaching up to 15.6% in terms of reduced total energy consumption, up to 20.6% in terms of per-SBS network delay reduction, and can reduce up to 69.9% the total cost.

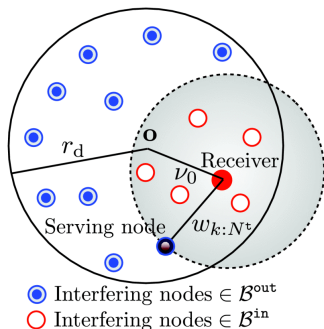




# 3. Fundamentals of Modeling Finite Wireless Networks Using Binomial Point Process

Authors: Mehrnaz Afshang, and Harpreet S. Dhillon

**Goal:** Establish a generic mathematical framework to characterize the performance of an arbitrarily located reference receiver in a finite wireless network (based on two TX-selection policies).



- **TX selection policy**
  - Uniform - ad hoc networks
  - $k$ -closest - Cellular networks
- **Locations of serving nodes** - Uniform BPP in a finite ball of radius  $r_d$
- Assume noise negligible compared to interference

- PDF of TX locations

$$f(\mathbf{y}_i) = \begin{cases} \frac{1}{\pi r_d^2} & \|\mathbf{y}_i\| \leq r_d \\ 0 & \text{otherwise.} \end{cases}$$

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- TX-Selection Policies and Propagation Model

$$\text{SIR} = \frac{h_\ell \|\mathbf{x}_0 - \mathbf{y}_\ell\|^{-\alpha}}{\sum_{\mathbf{y}_i \in \Phi_a \setminus \mathbf{y}_\ell} h_i \|\mathbf{x}_0 - \mathbf{y}_i\|^{-\alpha}},$$

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- Coverage Probability

$$P_c = \mathbb{E}[\mathbf{1}\{\text{SIR} \geq \beta\}] = \mathbb{P}(\text{SIR} \geq \beta),$$



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- **Coverage Probability**

$$P_c = \mathbb{E}[\mathbf{1}\{\text{SIR} \geq \beta\}] = \mathbb{P}(\text{SIR} \geq \beta),$$

- **Sequence of distances from TX to RX**

$$\text{PDF : } f_{W_i}(w_i) = \frac{2w_i}{r_d^2}; \quad 0 \leq w_i \leq r_d$$

- **Conditional PDF of the sequence**

$$f_{W_i}(w_i|\nu_0) = \begin{cases} f_{W_{i,1}}(w_i|\nu_0), & 0 \leq w_i \leq r_d - \nu_0 \\ f_{W_{i,2}}(w_i|\nu_0), & r_d - \nu_0 < w_i \leq r_d + \nu_0, \end{cases}$$

where  $f_{W_{i,1}}(w_i|\nu_0) = \frac{2w_i}{r_d^2}$  and  $f_{W_{i,2}}(w_i|\nu_0) = \frac{2w_i}{\pi r_d^2} \arccos\left(\frac{w_i^2 + \nu_0^2 - r_d^2}{2\nu_0 w_i}\right)$

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- **Coverage Prob - Uniform TX-Selection Policy**

$$\begin{aligned} P_{\text{ref}}^{(u)}(\nu_0) &= \int_0^{r_d - \nu_0} \mathcal{L}_{\mathcal{I}}^{(u)}(\beta r^\alpha | \nu_0) f_{W_{i,1}}(r | \nu_0) dr \\ &\quad + \int_{r_d - \nu_0}^{r_d + \nu_0} \mathcal{L}_{\mathcal{I}}^{(u)}(\beta r^\alpha | \nu_0) f_{W_{i,2}}(r | \nu_0) dr, \end{aligned}$$

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- **Coverage Prob -  $k$ -closest TX-Selection Policy**

$$\begin{aligned} P_{\text{ref}}^{(k)}(\nu_0) &= \int_0^{r_d - \nu_0} \mathcal{A}(\beta r^\alpha, r, \nu_0) f_{R,1}^{(k)}(r|\nu_0) dr \\ &\quad + \int_{r_d - \nu_0}^{r_d + \nu_0} \mathcal{B}(\beta r^\alpha, r, \nu_0) f_{R,2}^{(k)}(r|\nu_0) dr, \end{aligned}$$

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## Extensions of work:

- Modeling - analyze Matern cluster process.
- Systems - performance analysis of indoor communication and hotspots.
- Study performance of mmWave communication systems with receiver experiencing blocking interference.



## Other Interesting Papers

-  **Low-Rank Spatial Channel Estimation for Millimeter Wave Cellular Systems.**  
*Parisa A. Elias, Sundeep Rangan, and Theodore S. Rappaport*
-  **MIMO Energy Harvesting in Full-Duplex Multi-User Networks.**  
*Ho Huu Minh Tam, Hoang Duong Tuan, Ali Arshad Nasir, Trung Q. Duong, and H. Vincent Poor*
-  **Proactive Eavesdropping via Cognitive Jamming in Fading Channels.**  
*Jie Xu, Lingjie Duan, and Rui Zhang*
-  **Joint Precoding and RRH Selection for User-Centric Green MIMO C-RAN.**  
*Cunhua Pan, Huiling Zhu, Nathan J. Gomes, and Jiangzhou Wang*
-  **Load Optimization With User Association in Cooperative and Load-Coupled LTE Networks.**  
*Lei You and Di Yuan*