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- The Degrees of Freedom of MIMO Networks With Full-Duplex Receiver Cooperation but no CSIT

Authors: Chinmay S. Vaze and Mahesh K. Varanasi

# System Model

- MIMO IC with receiver cooperation

$$Y_1(t) = H_{11}(t)X_1(t) + H_{12}(t)X_2(t) + G_{12}(t)X_{R2}(t) + W_1(t)$$

$$Y_2(t) = H_{21}(t)X_1(t) + H_{22}(t)X_2(t) + G_{21}(t)X_{R1}(t) + W_2(t)$$

- MIMO BC with receiver cooperation

$$Y_1(t) = H_1(t)X(t) + G_{12}(t)X_{R2}(t) + W_1(t)$$

$$Y_2(t) = H_2(t)X(t) + G_{21}(t)X_{R1}(t) + W_2(t)$$

- Each receiver has perfect knowledge of all channel metrics, except of the one cooperative link which originates from it to the other receiver
- Full-duplex receiver cooperation
- No CSIT

# Results

- In general for IC with no receiver cooperation,

$$\mathbf{D}^{\text{no}} \subseteq \mathbf{D}^{\text{d}} \subseteq \mathbf{D}^{\text{S}} \subseteq \mathbf{D}^{\text{p\&i}} = \mathbf{D}^{\text{coop}}$$

- With perfect and instantaneous CSIT, receiver cooperation doesn't enhance the DoF, compared to half-duplex receivers.
- With no CSIT receiver cooperation appears to yield most of the gains promised by delayed CSIT, or even Shannon feedback.
- DoF benefits with receiver cooperation are realized using *retro-cooperative* interference alignment scheme.
- These schemes are DoF-region optimal for certain classes of MIMO ICs and BCs
- The outer bounds provided for DoF do not appear to be tight for unequal number of antennas at the receiver.

## ■ Feasibility of Interference Alignment for the MIMO Interference Channel

Authors: Guy Bresler, Dustin Cartwright and David Tse

# System Model

- K-user MIMO interference channel
- **Cadambe and Jafar:** For time-varying or frequency selective channels with *unbound diversity*, total degrees of freedom are  $\frac{K}{2}$ , i.e., DoF/per-user *independent* of  $K$ .
- How diversity affects the ability to align interference?
- **Goal:** Impact of spatial diversity on interference alignment
- No time or frequency diversity
- Linear precoding scheme

# Results

- **Problem Statement:** Given a number of user  $K$ , number of antennas  $M_1, \dots, M_K$  and  $N_1, \dots, N_K$ , and desired subspace dimensions  $d_1, \dots, d_K$ . Find subspaces  $U_1, \dots, U_K$  with the desired dimensions s.t.

$$\mathbf{H}^{[ij]} U_j \perp U_i, 1 \leq i, j \leq K, i \neq j$$

- Total degrees of freedom with only spatial diversity is **two**.
- Necessary conditions for alignment and a achievable linear precoding scheme is provided for symmetric  $K = 3$ .
- For  $K \geq 3$ ,  $d_i = d$ , and  $M_i = N_i = N$  for all users  $i$ , there is a feasible strategy iff  $2N \geq (K + 1)d$
- Achievable DoF for fully symmetric is also provided.

- An Improved RIP-based Performance Guarantee for Sparse Signal Recovery Via Orthogonal Matching Pursuit

Authors: Ling-Hua Chang and Jwo-Yuh Wu



# Earlier Result

- Signal model:

$$\mathbf{y} = \Phi \mathbf{x} + \mathbf{w}$$

- OMP with stopping criteria
- Wu, Huang, and Chen, 2013

- 1 ( $\ell_2$ -bounded noise): Under  $\|\mathbf{w}\|_2 \leq \epsilon_1$ , and stopping criterion  $\|\mathbf{r}^j\|_2$ , the support of the  $K$ -sparse signal  $\mathbf{x}$  can be identified if  $\delta_{K+1} < \frac{1}{\sqrt{K+1}}$  and the non zero entries satisfies

$$\min_{i \in T} |(\mathbf{x})_i| > \frac{(\sqrt{1 + \delta_{K+1}} + 1)\epsilon_1}{1 - \delta_{K+1} - \sqrt{K}\delta_{K+1}}$$

- 2 ( $\ell_\infty$ -bounded noise): If  $\|\Phi^* \mathbf{w}\|_\infty \leq \epsilon_2$ , and stopping criteria  $\|\Phi^* \mathbf{r}^j\|_\infty \leq \epsilon_2$ , then for exact support recovery

$$\min_{i \in T} |(\mathbf{x})_i| > \frac{(\sqrt{\delta_{K+1}} + 1)\sqrt{K}\epsilon_2}{1 - \delta_{K+1} - \sqrt{K}\delta_{K+1}}$$

# Improved Results

1 ( $\ell_2$ -bounded noise):  $\delta_{K+1} < \frac{\sqrt{4K+1}-1}{2K}$  and

$$\min_{i \in T} |(\mathbf{x})_i| > \frac{(\sqrt{1+\delta_{K+1}}+1)\epsilon_1}{1-\delta_{K+1}-\sqrt{1-\delta_{K+1}}\sqrt{K}\delta_{K+1}}$$

2 ( $\ell_\infty$ -bounded noise):  $\min_{i \in T} |(\mathbf{x})_i| > \frac{(\sqrt{K}+1)\epsilon_2}{1-\delta_{K+1}-\sqrt{1-\delta_{K+1}}\sqrt{K}\delta_{K+1}}$

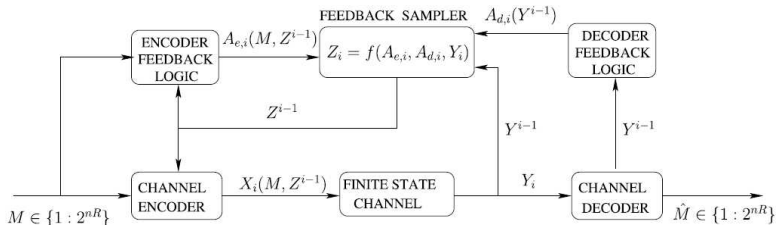
- In noiseless case, it ensures exact support recovery in  $K$  iteration.
- *Near-Orthogonality* condition: Let  $\mathbf{u} \perp \mathbf{v}$  s.t.  $|T_u \cup T_v| \leq K$ , and  $\Phi$  satisfies RIP of order  $K$  with RIC  $\delta_K$ . Then

$$|\cos \angle(\Phi_{\mathbf{u}}, \Phi_{\mathbf{v}})| \leq \delta_K$$

## ■ To Feed or Not to Feedback

Authors: H. Asnani, H. H. Permuter, and T. Weissman

# Setup



The codes satisfy the cost constraint

$$E \left[ \Lambda \left( A_e^N, A_d^N \right) \right] = E \left[ \frac{1}{N} \sum_{i=1}^N \Lambda \left( A_{e,i}, A_{d,i} \right) \right] \leq \Gamma$$

# Contributions

- Exactly characterize the capacity of finite state channels when  $P(s_0) > 0, \forall s_0$
- Capacity of indecomposable FSC without ISI
- Blahut-Arimoto algorithm is provided for the case when actions are cost-constrained.
  - To feed or not to feedback
- Characterization of capacity using a dynamic programming formulation

# Other Papers

- *“Compress-and-Forward Scheme for Relay Networks: Backward Decoding and Connection to Bisubmodular Flows”*, A. Raja and P. Viswanath
- *“Index Coding - An Interference Alignment Perspective”*, H. Maleki, V. R. Cadambe, and S. A. Jafar
- *“Private Broadcasting over Independent Parallel Channels”*, A. Khisti and T. Liu
- *“Fading Channels With Arbitrary Inputs: Asymptotics of the Constrained Capacity and Information and Estimation Measures”*, A. G. C. P. Ramos and M. R. D. Rodrigues