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### Optimal Phase Transitions in Compressed Sensing

Authors: Y. Wu and S. Verdu Affiliations: Department of Statistics, The Wharton School, University of Pennsylvania, USA and Department of Electrical Engineering, Princeton University, USA

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- Goal: To investigate the fundamental tradeoff between reconstruction fidelity and measurement rate  $(\frac{k}{n})$
- Phase transitions (for noiseless measurement): For many input processes (i.i.d. ones), there exits a threshold *d*(*X*) such that:
  - When *R* > *d*(*X*), it is possible to achieve vanishing error probability
  - When  $R \leq d(X)$ , error probability approach 1
- Phase transitions (for noisy measurement): Noise sensitivity is considered to analyze reconstruction fidelity

System model

$$\mathbf{P}_{\mathbf{X}} = (\mathbf{1} - \gamma)\mathbf{P}_{\mathbf{d}} + \gamma \mathbf{P}_{\mathbf{c}}$$

where  $P_d$  and  $P_c$ : discrete and cont. prob. measure

- For i.i.d. discrete-continuous mixtures: minimal measurement rate is given by the input information dimension, i.e., the weight of the absolutely continuous part (γ)
- Measurements corrupted by additive Gaussian noise:
  - optimal nonlinear encoder
  - optimal linear encoder
  - random linear encoder
- When input is i.i.d.: for any input distribution, the phase transition threshold for optimal encoding is given by the input information dimension  $d(X) = \lim_{m \to \infty} \frac{H(\lfloor m \mathbf{X} \rfloor)}{\log m}$
- Look the paper for following three dimensions
  - Information dimension
  - MMSE dimension
  - Minkowski dimension

#### Sum rate of the Vacationing CEO problem

Authors: Rajiv Soundararajan, Aaron B. Wagner, and Sriram Vishwanath Affiliations: Department of Electrical and Computer Engineering, The University of Texas at Austin, USA and School of Electrical and Computer Engineering, Cornell University, USA

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- Vacationing CEO problem: multiple encoders compress noisy versions of a single source in a distributed manner
- Combination of
  - 1. CEO problem
  - 2. multiple description (MD) problem



- Achievable scheme: Berger-Tung scheme for multiterminal source coding and the El Gamal-Cover scheme for MDs
- Gaussian scheme is optimal in the low distortion regime
- Time-sharing scheme with Gaussian codebooks is optimal in the high distortion regime

## Achieving AWGN Capacity Under Stochastic Energy Harvesting

Authors: O. Ozel and S. Ulukus

Affiliations: Department of Electrical and Computer Engineering, University of Maryland, USA

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- To analyze point-to-point communication of energy harvesting nodes from an information-theoretic perspective
- For continuous alphabet channel:
  - 1. average power constraint
  - 2. amplitude constraint
- Energy arrives at transmitter as discrete time stochastic process
- Cumulative power constraint:  $\sum_{i=1}^{k} X_i^2 \le \sum_{i=1}^{k} E_i, i = 1, ... n$



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• Main result:

The capacity of an AWGN channel with cumulative power constraint = classical AWGN capacity with average power constraint

- Achievable scheme
  - 1. Save and transmit
  - 2. Best effort transmit scheme
- Also, considers a system in which the average recharge rate is time varying in a larger time scale
- Optimization problem: Majorization and Schur convexity

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# On the Optimality of Binning for Distributed Hypothesis Testing

Authors: M. Rahman and A. B. Wagner Affiliations: School of Electrical and Computer Engineering, Cornell University, USA

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• Vector source  $(X_1, \dots, X_L, Y)$  has joint distribution

$$H_0: P_{\mathbf{X}_1,...,\mathbf{X}_L,\mathbf{Y}}$$
$$H_1: P_{\mathbf{X}_1,...,\mathbf{X}_L,\mathbf{Y}}$$

### Objective

- Characterize all achievable encoding rates
- Exponents of Type 2 error when Type 1 error is at most a fixed value

- Consider a class of *L*-encoder hypothesis testing problem against conditional independence
- Achievable scheme: Quantize-bin test
  - Encoder *I* first quantizes X<sup>n</sup><sub>l</sub> by selecting a codeword U<sup>n</sup><sub>l</sub> that is jointly typical with it

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- Encoder then sends index of the bin
- Provides outer bound for more general class of problem