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Designing Incoherent Frames Through Convex Techniques for Optimized Compressed Sensing

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Definition

A family of vectors $F = \{f_i\}_{i=1}^N$ in \mathbb{R}^m is called a frame for \mathbb{R}^m , if there exist constants $0 < A \leq B < \infty$ such that

$$A \|x\|^{2} \leq \sum_{i=1}^{n} |\langle x, f_{i} \rangle|^{2} \leq B \|x\|^{2}$$
(1)

- If A = B, then F is an A-tight frame.
- If $||f_i|| = 1$ for all *i* and if there exist $\alpha \ge 0$ such that $|\langle f_i, f_j \rangle| = \alpha$ for all $i \ne j$ then *F* is an Equiangular
- Grassmannian frame is one that minimizes the maximal correlation $\langle f_i, f_j \rangle$ among all frames $F = \{f_i\}_{i=1}^N$

- Mutual coherence of a frame is largest absolute inner-product between different normalized elements of *F*
- This paper is concerned the problem of designing real frames with low mutual coherence
- One can find the solution for above mentioned problem by solving the following Optimization problem:

$$min_{\{F\}}max_{\{i \neq j\}}|\langle f_i, f_j \rangle| \text{ s. } t ||f_i||_2 = 1 \text{ for all } i$$
 (2)

- The authors have proceed to relax this problem and provide convex optimization formulations to solve it approximately
- The approach taken in this paper is for given a frame $H = \{h_i\}_{i=1}^N$ to find a new frame $F = \{f_i\}_{i=1}^N$ that is near to the initial one, with smaller mutual coherence by solving the following convex optimization problem: For all i = 1, ..., N

$$\min_{\{f_i; \|f_i - h_i\|_2^2 \le T_i\}} \max_{\{j; j \ne i\}} |\langle h_j, f_i \rangle|$$
(3)

Enhanced Sparsity by Non-Separable Regularization

Ivan W. Selesnick and Iker Bayram

- The authors have developed a convex approach for sparse deconvolution that improves upon *I*₁-norm regularization
- They have posed the sparse deconvolution problem named as BISR in the following way:

$$\tilde{x} = \arg \min_{x \in \mathbb{R}^2} \bigg\{ f(x) = \frac{1}{2} \|y - Hx\|_2^2 + \lambda \Psi(x) \bigg\}, \qquad (4)$$

where, $\lambda > 0$ and $\Psi(x) : \mathbb{R}^2 \to \mathbb{R}$ is a penalty function.

- This method is based on designing a non-convex penalty function Ψ(x) so that the objective function is convex
- The new penalty overcomes limitations of separable regularization.
- They have given an algorithm for above mentioned problem. Further, this bivariate problem has been extended to an *N*-point linear inverse problem

Compressed nonnegative matrix factorization is fast and accurate

Mariano Tepper and Guillermo Sapiro

- In recent years, Nonnegative Matrix Factorization (NMF) has been frequently used since it provides a good way for modeling many real-life applications
- NMF seeks to represent a nonnegative matrix as the product of two nonnegative matrices
- One can find the solution of NMF by solving the following optimization problem:

$$\min_{\{X \in \mathbb{R}^{m \times r}, Y \in \mathbb{R}^{r \times n}\}} \|A - XY\|_F^2 \text{ s. } t X, Y \ge 0$$
(5)

where r is a parameter that controls the size of factors X and Y and, hence, the factorization's accuracy.

• In the general case, NMF is known to be NP-Hard

- However, there are matrices that exhibit a particular structure such that NMF can be solved efficiently
- A nonnegative matrix A is r-separable if there exists an index set K of cardinality r over the columns of A and a nonnegative matrix Y ∈ ℝ^{r×n}, such that A = (A)_{:K}Y
- When A presents this type of special structure, the NMF problem (now denoted as separable NMF, SNMF) can be simply modeled as

 $\min_{\{\mathcal{K}\subset\{1,\ldots,n\},\,Y\in\mathbb{R}^{r\times n}\}}\|A-(A)_{:\mathcal{K}}Y\|_{F}^{2}\text{ s. }t \ |\mathcal{K}|=r,\,Y\geq 0 \ (6)$

- The goal of this paper is to develop algorithms, based on structured random projections, for computing NMF for big data matrices
- The authors have showed that the resulting compressed techniques are faster than their uncompressed variants, vastly reduce memory demands

- Analysis of a Subset Selection Scheme for Wireless Sensor Networks in Time-Varying Fading Channels by S. H. Mousavi, et.al.
- Collaborative Multi-Sensor Classification Via Sparsity-Based Representation by M. Dao, et.al.

Thank you