

E8-202 CEM Class 1.

Slide A

- E Electric Field (V/m)
- H Magnetic Field (A/m)
- D Electric Flux density (coulombs/m²)
- B Magnetic Flux density (W/m²)
- J Electric current density (A/m²)

$$V \longleftrightarrow E$$

$$I \longleftrightarrow H$$

$$\nabla \times \vec{V} \rightarrow \begin{bmatrix} \hat{x} & \hat{y} & \hat{z} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ V_x & V_y & V_z \end{bmatrix} \text{ curl.}$$

$$\nabla \cdot \vec{V} \rightarrow \begin{bmatrix} \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \end{bmatrix} \begin{bmatrix} V_x \\ V_y \\ V_z \end{bmatrix} \text{ div.}$$

$$\nabla s \rightarrow \hat{x} \frac{\partial s}{\partial x} + \hat{y} \frac{\partial s}{\partial y} + \hat{z} \frac{\partial s}{\partial z} \text{ grad.}$$

Slide 5

$$\nabla \times E = -j\omega B$$

$$\nabla \times H = j\omega D + J$$

$$\nabla \cdot D = \rho$$

$$\nabla \cdot B = 0$$

F, D.

$$\iint_S (\nabla \times E) \cdot ds = \iint_S \left(-\frac{\partial B}{\partial t} \right) ds$$

$$\Rightarrow \oint_{dl} E \cdot dl = \iint_S \left(-\frac{\partial B}{\partial t} \right) ds$$

$$\oint_{dl} H \cdot dl = \iint_S \left(\frac{\partial D}{\partial t} \right) ds + \iint_S J$$

$$\iint_S D \cdot ds = \iiint_V \rho \, dv$$

$$\iint_S B \cdot ds = 0$$

slides :-

$$D = \epsilon E$$

$\epsilon \rightarrow$ permittivity
(F/m)

$$C = \frac{A\epsilon}{d} \quad \epsilon = \frac{Cd}{A}$$

$$\epsilon = \frac{D}{E}$$
$$\frac{\text{Coulomb/m}^2}{\text{V/m}}$$
$$= \text{Farads/m}$$

$$B = \mu H$$

$$\downarrow$$
$$\text{H/m}$$

$$\text{J} = \sigma E$$
$$\downarrow$$
$$\text{S/m}$$

$$C = \frac{1}{\sqrt{\mu\epsilon}}$$

$$\eta = \sqrt{\frac{\mu}{\epsilon}}$$

intrinsic impedance.

(Displacement current, conduction current, ~~incident~~ imposed current)

Homogeneous \rightarrow
Nonlinear \rightarrow plasma.
Anisotropic \rightarrow sapphire

Slide 8:-

$$\nabla \times H = j\omega \cancel{D} + \cancel{J_c} + J_i$$

$$= j\omega \epsilon_0 \epsilon_r \cancel{D} E + \sigma E + J_i$$

$$= j\omega \epsilon_0 \epsilon_c E + J_i$$

$$\epsilon_0 \epsilon_c = \left(\epsilon_0 \epsilon_r + \frac{\sigma}{j\omega} \right)$$

$$\left[\epsilon_c = \epsilon_r - j \frac{\sigma}{\epsilon_0 \omega} \right]$$

$$\epsilon_c = \epsilon_r - j \epsilon_{imag}$$

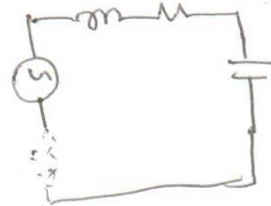
$$\tan \delta = \frac{\epsilon_{imag}}{\epsilon_{real}}$$

Slide 9 :-

$$\nabla \times E = - \frac{\partial B}{\partial t}$$

$$\sum v = \oint E \cdot dl = - \frac{\partial}{\partial t} \iint B \cdot ds$$

$$-v_s + v_R + v_L + v_C = - \frac{\partial \Psi_m}{\partial t} = L_s \frac{di}{dt} = -v_{sL}$$

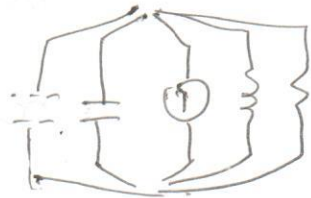


$$\nabla \cdot J = - \frac{\partial \rho}{\partial t}$$

$$\oint J \cdot ds = - \iint \frac{\partial \rho}{\partial t} \cdot dv$$

$$\sum i = - \frac{\partial Q}{\partial t} = - \frac{\partial \sum v}{\partial t} = - C_s \frac{\partial v}{\partial t}$$

$$-i_s + i_R + i_L + i_C = - C_s \frac{\partial v}{\partial t}$$



Full wave :-



$$P = \frac{1}{f}$$

$$t_r = \frac{P}{10} = \frac{1}{10f}$$



$$t_d = \frac{l}{c}$$

$$t_d \gg t_r$$

$$\frac{l}{c} \gg \frac{1}{10f}$$

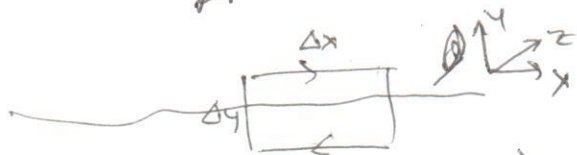
$$l \gg \frac{\lambda}{10}$$

Slide 10 :-

$$n \times (H_2 - H_1) = J_s$$

$$n \times m \cdot (D_2 - D_1) = \Phi_{res}$$

$$\oint H \cdot dl = \frac{d}{dt} \oint B \cdot ds = \oint J \cdot ds$$



$$(H_1 - H_2) \cdot \hat{a}_x \Delta x = J \cdot \hat{a}_z \Delta x \Delta y - J \Delta y \cdot \hat{a}_z \Delta x$$