

1. Consider an  $N \times N$  VOQ switch where the arrival process into the queue  $(i, j)$  is Bernoulli with mean  $\lambda_{ij}$ . Assume that  $\sum_i \lambda_i k < 1$  and  $\sum_j \lambda_{ij} \forall k, l$ . Compute an upper bound on the steady state mean of the sum of the queue lengths in the network assuming that the MaxWeight scheduling algorithm is used.
2. Consider a  $2 \times 2$  VOQ switch. The arrival process into VOQ $(i, j)$  is Bernoulli with mean  $\lambda_{ij}$ . The arrival processes are independent across queues and time slots. Consider a scheduling policy that gives priority to edges  $(1, 2)$  and  $(2, 1)$ , i.e., these links are scheduled if they have any packets in their queues. Given  $\lambda_{12}$  and  $\lambda_{21}$ , compute the set of  $(\lambda_{11}, \lambda_{22})$  that can be supported under the priority scheduling policy above and the set of  $(\lambda_{11}, \lambda_{22})$  that can be supported by the MaxWeight scheduling algorithm. Assume that  $q_{12}(0) = q_{21}(0) = 0$ .
3. Consider the network shown in Figure 1. All links of this network are bi-directional links, i.e.,  $c_{ij} = c_{ji}$  for all  $i$  and  $j$ . The numbers in the figure are the link costs. Compute and summarize the result of Dijkstra's algorithm (at node  $a$ ) at the end of each iteration

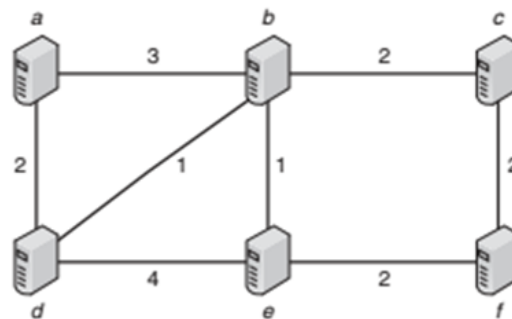


Figure 1: Network configuration

4. Consider a single wireless link, which can be in one of two states indexed by  $m = 0, 1$ . The transmitter has two power levels, indexed by  $j = 0, 1$ , such that  $p_0 = 1$  and  $p_1 = 5$ . The maximum number of packets that can be transmitted over the link under different channel states and transmit powers are summarized in Table-1. Assume that two-channel states occur equally likely, i.e.,  $\pi_0 = \pi_1 = 0.5$ .

|           | $m = 0$ (bad) | $m=1$ (good) |
|-----------|---------------|--------------|
| $P_0 = 1$ | 1             | 2            |
| $P_1 = 5$ | 3             | 5            |

- a. Let  $\alpha_{m,j}$  denote the fraction of time that the transmitter transmits at power level  $j$  when the channel is in state  $m$ . Given  $\alpha_{00} + 5\alpha_{01} = x$  for  $0 \leq x \leq 5$ , i.e., the average transmit power when the channel is in state 0 is  $x$ , calculate the maximum achievable throughput when the channel is in state 0, i.e.,  $\max \alpha_{00} + 3\alpha_{01}$  subject to  $\alpha_{00} + 5\alpha_{01} = x$ .
- b. Given  $\alpha_{10} + 5\alpha_{11} = y$  for  $0 \leq y \leq 5$ , i.e., the average transmit power when the channel is in state 1 is  $y$ , calculate the maximum achievable throughput when the channel is in state 1, i.e.,  $\max 2\alpha_{10} + 5\alpha_{11}$  subject to  $\alpha_{10} + 5\alpha_{11} = y$ .